

6 • Energy and Chemical Reactions

CALORIMETRY

Measuring heat (formerly measured in calories) is called **calorimetry**. Now we measure heat energy in Joules (J). The equation we use is:

$$q = m \cdot C \cdot \Delta T$$

q = heat energy

m = mass of water

C = the specific heat capacity

ΔT = the change in temperature (in $^{\circ}\text{C}$ or K)

1. Water has a specific heat capacity of $4.184 \text{ J/g}\cdot^{\circ}\text{C}$.

This means it takes 4.184 J to heat 1.00 gram of water 1.00°C .

- a) How much energy will it take to heat 10.0 grams of water 1°C ? 41.84 J
 b) How much energy is needed to heat $30.0 \text{ g H}_2\text{O}$ from 10.0°C to 50.0°C ? 5020.8 J

$$q = (30.0 \text{ g}) \left(\frac{4.184 \text{ J}}{\text{g}\cdot^{\circ}\text{C}} \right) (40.0^{\circ}\text{C}) = \underline{5020.8 \text{ J}}$$

2. Let's try a standard **calorimetry** problem.

A pot of water (2.5 Liters of water) initially at 25.0°C is heated to boiling (100.0°C). $2.5 \text{ L} \times \frac{1000 \text{ mL}}{1 \text{ L}} \times \frac{1 \text{ g}}{1 \text{ mL}} = 2500 \text{ g}$
 How much energy (in J) is needed to heat the water? (The density of water is 1 g/mL .)

$$q = (2500 \text{ g}) \left(\frac{4.184 \text{ J}}{\text{g}\cdot^{\circ}\text{C}} \right) (75.0^{\circ}\text{C}) = \underline{784500 \text{ J}} = \underline{780000 \text{ J}}$$

What would this amount of heat be in kJ? $784.5 \text{ kJ} = \underline{780 \text{ kJ}}$ 2 sig. figs.

3. What amount of heat is *released* when 175 g of water *cools* from 100.0°C to room temperature, 20.0°C ?

$$q = (175 \text{ g}) \left(\frac{4.184 \text{ J}}{\text{g}\cdot^{\circ}\text{C}} \right) (-80.0^{\circ}\text{C}) = -58576 \text{ J} = -58.6 \text{ kJ} = \underline{-59 \text{ kJ}}$$

⊖ sign mean heat is given OFF.

4. We don't always have to warm up or cool down water. The specific heat capacity of copper metal is $0.39 \text{ J/g}\cdot^{\circ}\text{C}$. It is easier (easier/more difficult) to heat up copper than to heat up water.

How much energy would it take to heat up a 5.20 g sample of copper from 20.0°C to 100.0°C ?

$$q = (5.20 \text{ g}) \left(\frac{0.39 \text{ J}}{\text{g}\cdot^{\circ}\text{C}} \right) (80.0^{\circ}\text{C}) = 162.24 \text{ J} = \underline{160 \text{ J}}$$

5. If $300. \text{ J}$ of heat energy were used to heat up a 5.00 gram sample of copper metal and a 5.00 gram sample of water both starting at 10.0°C , calculate the final temperature of each sample?

Cu $q = m c \Delta T$

$$300 \text{ J} = (5.00 \text{ g}) \left(\frac{0.39 \text{ J}}{\text{g}\cdot^{\circ}\text{C}} \right) \Delta T$$

$$\Delta T = \Delta T = \frac{(300)}{(5)(0.39)} = 154^{\circ}$$

$T_f = 164^{\circ}\text{C}$

H₂O $q = m c \Delta T$

$$300 \text{ J} = (5.00 \text{ g}) \left(\frac{4.184 \text{ J}}{\text{g}\cdot^{\circ}\text{C}} \right) \Delta T$$

$$\Delta T = \Delta T = \frac{(300)}{(5.00)(4.184)} = 14.3^{\circ}$$

$T_f = 24.3^{\circ}$

Signs of ΔT and q :

– q means heat is **released**. + q means heat is **absorbed**.

ΔT is always **final** temperature – **initial** temperature.

If something is getting **hotter** ($10^\circ \rightarrow 30^\circ$) the ΔT is $30 - 10 = +20^\circ$. (heat is **absorbed**)

If something is getting **cooler** ($75^\circ \rightarrow 25^\circ$) the ΔT is $25 - 75 = -50^\circ$. (heat is **released**)

6. Suppose we mix 90.0 grams of **hot water** (90.0°C) with 10.0 grams of **cold water** (10.0°C).

Let x = the final temperature. $C = 4.184 \text{ J/g}\cdot^\circ\text{C}$

- a. Set up an expression for the energy **released** (q) by the hot water ($\Delta q_{\text{hot}} = m_{\text{hot}}C\Delta T_{\text{hot}}$)

$$q = (90.0\text{g})(4.184 \frac{\text{J}}{\text{g}\cdot^\circ\text{C}})(x - 90.0^\circ\text{C})$$

- b. Set up an expression for the energy **absorbed** (q) by the cold water ($\Delta q_{\text{cold}} = m_{\text{cold}}C\Delta T_{\text{cold}}$)

$$q = (10.0\text{g})(4.184)(x - 10.0^\circ\text{C})$$

- c. Knowing that the heat released = – heat absorbed, combine the two expressions and solve for x .

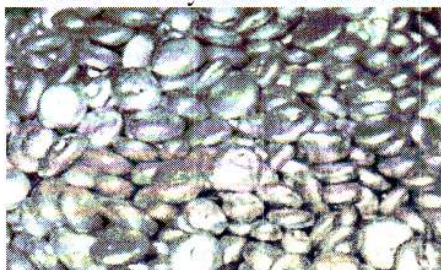
Hot $q = -q_{\text{cold}}$

$$(90)(4.184)(x - 90) = -(10)(4.184)(x - 10)$$

$$90x - 8100 = -10x + 100$$

$x = 82^\circ\text{C}$

7. We don't always have to use water. Let's use some **aluminum shot**.



"shot" are these little pellets.

175 grams of hot aluminum ($100.^\circ\text{C}$) is dropped into an insulated cup that contains 40.0 mL of ice cold water (0.0°C). Follow the example above to determine the final temperature, x .

- a. Set up an expression for the heat lost by the aluminum

$$(C=0.900 \text{ J/g}\cdot^\circ\text{C}) \quad q = (175\text{g})(.900 \frac{\text{J}}{\text{g}\cdot^\circ\text{C}})(x - 100.^\circ\text{C})$$

- b. Set up an expression for the heat gained by the cold water.

$$q = (40.0\text{g})(4.184 \frac{\text{J}}{\text{g}\cdot^\circ\text{C}})(x - 0.0^\circ\text{C})$$

- c. Put the two expressions together (don't forget to change one of the signs) and solve for x .

Hot $q = -q_{\text{H}_2\text{O}}$

$$(175)(.9)(x - 100) = -(40)(4.184)(x - 0)$$

$$157.5x - 15750 = -167.4x + 0$$

$$+167.4x \quad +15750$$

$$324.9x = 15750$$

$x = 48.5^\circ$

8. **Somewhat Confusing Definitions:**

There are several terms used in this chapter that sound very similar. Use the data provided to calculate each of them to clarify the differences. I've added some "Notes" that I hope will help.

74.8 J of heat is required to raise the temperature of 18.69 g of silver from 10.0°C to 27.0°C .

- a. What is the **heat capacity** of the silver sample? ($\text{J}/^\circ\text{C}$)

Note: This is a useful value only for this specific sample of silver.

$$\frac{74.8\text{J}}{17.0^\circ\text{C}} = \boxed{4.4 \frac{\text{J}}{^\circ\text{C}}}$$

$$\Delta T = 27.0 - 10.0 = 17.0^\circ\text{C}$$

- b. What is the **specific heat capacity** of silver? ($\text{J/g}\cdot^\circ\text{C}$)

Note: This is a useful value for **any** sample of silver that is heated or cooled. This is equivalent to the $4.184 \text{ J}\cdot\text{g}^{-1}\cdot^\circ\text{C}^{-1}$ that we use for water. This value is also called the **specific heat**.

$$\frac{74.8\text{J}}{(18.69\text{g})(17.0^\circ\text{C})} = \boxed{0.235 \frac{\text{J}}{\text{g}\cdot^\circ\text{C}}}$$